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, @83823#><%, @"; 8! 4@8%3163%@824:38! %#>%@8! 4; #><%318%"@#<#>6:%A6; 3"@2% lbhc h\fyy fl E dflbvldu Wa dcbybha 8 ydybxuvl lhm ubx 5 lluhlcb YNM[89M>=#8359#>9K"; #6:9K#3463#">9/M>=KK[896>! %i 82, ">2#C#:#35%i 82, [(% 8 YdYbXUV]`]mi UbX: 5 `]Uhjcb: fB5Ł: dYfhUjbg: hc: h\Y: ghfcb[Yf: gYbgY: cZ UXUdHUV]`]hm UbX`U `]Uh]cb cZ h\Y a UbUbU`c" 5bl ]Yhm ]b GcVW` K#3463#''>\|\M\>=KK\[B\|\@8A8\@2\|\3\\\8\\8\=#835B\\4#:3B\\8\\@9\\42\822B\\6\!\\?\\\@@5\\ 8=, 8@#8>; 8! %C5%18%76>6>6:"\#>\%2"; #6:\%#3463#">2(\% 82, ">2\#C\#:\#35\%i 82, [\% ! 82; @#C82%318%28>28%"A%; ">3@":B%@82, ">2#C#:#35B%6>! %#>! 8, 8>! 8>; 8%#>% 318%76>6>6:"%/h"%O#6>DC<8%U''/[%h"%O#6>DC<%\U''/[\%\"4>!\%\"?\%\\% 7"! 8@638%; "@@8:63#">2%C83?88>%318%1@88%) [%, @#76@5%; "7, ">8>32%"A% 318%!"#"\$"%&%2;6:8%;@8638!%C5%h6@;#6%6>!%318%F6>4H63%><%F6<H636"><% F#:#, #>"%YFFF[%"A%L6@:"36%Y&]]\*[(%%O18%96:#! #35%"A%318%2; 6:8%?62%>"3% 8236C:#218! (%O18%e824:32%6:2"%21"?8! %3163%C83?88>%<8>! 8e28%A876:82% 2; "@8! %1#<18@\\$>\\$18\\$1@88\\$6; 3\"@2\\h\"DO\\$6>B\U\'\[(\%O18\\\$\)=\\$3\#6:\%?\"@H\\"A\% 318%, 25; 1" 783@#; %2" 4>! >822%' A%!" #" \$" %&%2; 6:82(

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O18% XhN% <8>8e638! %e#; 1%#>A"@763#">%6C"43%318%@82, ">! 8>32%31"4<1328%88:#><28%>! %C8169#"@2%"A%C8#><%%"#"\$"%&(%g8A"@8%18%236@3%"A%18%! #2; 422#">B%, 6@3#; #, 6>32%?8@8%<#98>%6>##>A"@78! %; ">28>3%"@7% h\ Uh Yl d`U]bYX h\ Y' WtbÙXYbh]U` UbX j c`i bhUfmbUhi fY`cZ h\ Y`fYgYUfW\ 6>! %18#@#<13%"%?#31! @6?%6>53#78%?#31"43%8>6:35(%N4@#><%18%XhNB%, 6@3#; #, 6>32%?8@8%2H8! %1"?%C8#><%%1"#"\$"%&%76>#A8238! #>%18#@#\$982(%6"#"\$"%&%318782%3163%24@A6; 8! %#>%318%XhN%?8@8\$\%\&[%23@"><%4@<8%3"%622478\%82, ">2#C#:#35B%U[%C8#><%6%78! #63"@8%) [%@#"@#3#G#><%'318@2%'98@%28:AB%>! %/[#>; :#>63#">%"%6H8%6@8%"A%"318@2(%"78%"A%18\%28, ">282%'A%318\%XhN\%6@3#; #, 6>32\%216@8! \@163%

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